



Angular Kinetics



Parameters

- **Torque**
 - Definition
 - Units
- **Couple**
- **Center of Gravity (Mass)**
- **Moment of Inertia**
 - Steiner's Theorem or Parallel Axis Theorem
- **Angular Momentum (H)**



Newton's First Angular Law

The Law of Inertia

In the absence of an external torque exerted about a given axis, the angular momentum of a body about that axis remains constant.

Law of Inertia may be viewed as a special case of the 2nd Law.



Newton's Second Angular Law

The Law of Acceleration

The rate of change of angular momentum (H) of a body [$d(H)/dt$] is proportional to the net torque causing it and the change takes place in the direction the net torque acts.

$T_{NET} \equiv \Sigma T$ - Is the sum of all external torque acting upon the body

$$T_{NET} = \frac{d(H)}{dt} = \frac{d(I\omega)}{dt} = I \frac{d\omega}{dt} + \frac{dI}{dt} \omega$$

If the body is rigid, ($dI/dt = 0$) &

$$T_{NET} = \frac{d(H)}{dt} = I \frac{d\omega}{dt} + \frac{dI}{dt} \omega = I \frac{d\omega}{dt} = I\alpha$$



Newton's Second Angular Law

The Law of Acceleration

If an object has constant moment of inertia, we can state this Law as:

The angular acceleration of a body with constant moment of inertia is proportional to the net torque causing it and the change takes place in the direction the net torque acts.

$$\mathbf{T}_{NET} = I\alpha$$

$$\alpha = \mathbf{T}_{NET} / I$$



Newton's Second Angular Law

The Law of Acceleration

$$\mathbf{T}_{NET} = \frac{d(H)}{dt}$$

$$\mathbf{T}_{NET} dt = d(H)$$

$$\int_{t_1}^{t_2} \mathbf{T}_{NET} dt = \int_{H_1}^{H_2} dH$$

Angular Impulse = Change in Angular Momentum

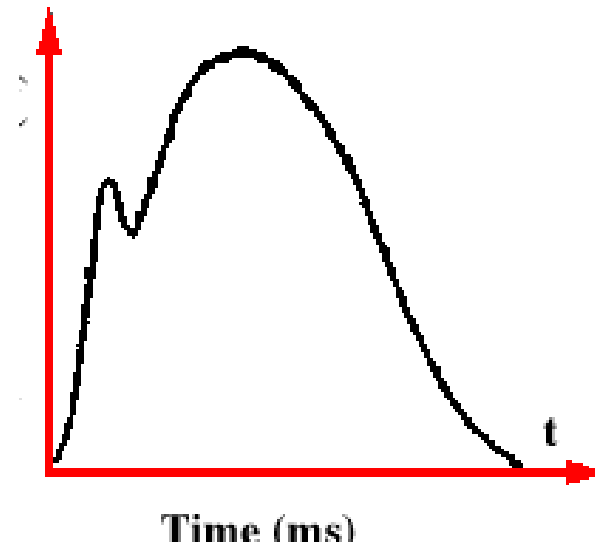
Newton's Second Law

The Law of Acceleration

Angular Impulse = Change in Angular Momentum

$$\int_{t_1}^{t_2} \mathbf{T}_{NET} dt = \int_{H_1}^{H_2} dH = (H_2 - H_1) = \Delta H_{1-2}$$

Area under the T_{NET} versus time graph between t_1 and t_2





Newton's Third Law Action & Reaction

When a body exerts a torque about a given axis, the second body exerts on the first body an equal and opposite torque about the same axis.

In other words, if object A exerts a torque on object B, then object B also exerts an equal and opposite torque on object A.